

High redshift deuterium abundance

Resolving the tension between quasar and CMB Ω_b measurements

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Outline

Motivation

Voigt Function

Kramers-Heisenberg Formula

Voigt & K-H

Outline

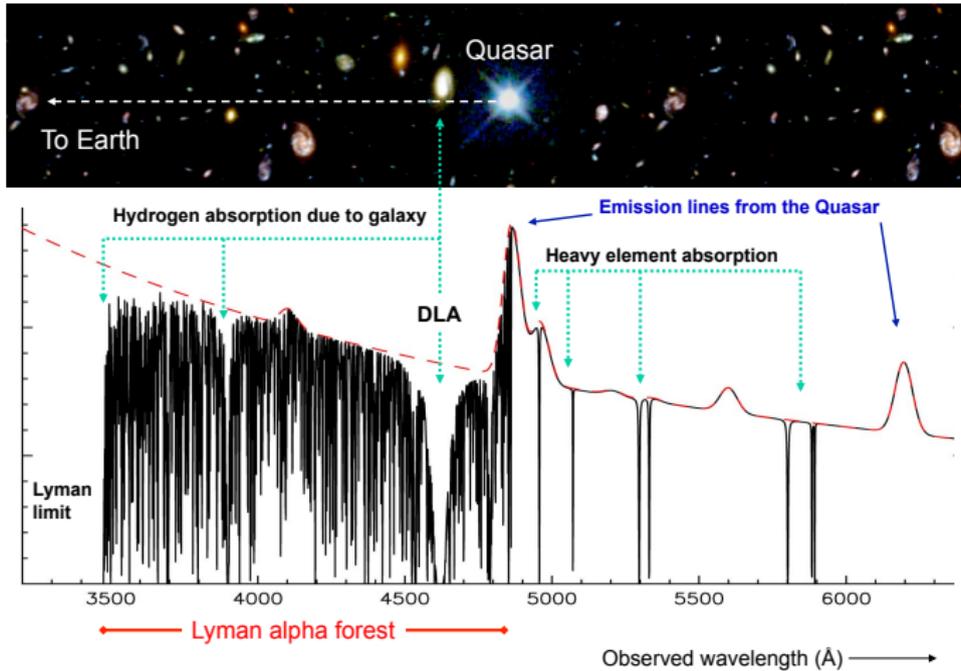
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Table 4. The sample of D I/H I measurements considered robust in Pettini et al. (2008) together with updated estimates in the same absorbers and more recent, similarly precise measurements from other absorbers.

Reference	Absorption redshift	$\log(N(\text{H I}))$	[X/H]	D I/H I [$\times 10^{-5}$]	$100\Omega_b h^2$
Burles & Tytler (1998a)	2.504	17.4 ± 0.07	-2.55 Si	4.00 ± 0.70	1.66 ± 0.18
Pettini & Bowen (2001)	2.076	20.4 ± 0.15	-2.23 Si	1.65 ± 0.35	2.82 ± 0.36
Kirkman et al. (2003)	2.426	19.7 ± 0.04	-2.79 O	2.43 ± 0.35	2.24 ± 0.20
Fumagalli et al. (2011)	3.411	18.0 ± 0.05	-4.20 Si	2.04 ± 0.61	2.49 ± 0.05
Noterdaeme et al. (2012)	2.621	20.5 ± 0.10	-1.99 O	2.80 ± 0.80	2.05 ± 0.35
Cooke et al. (2014), Pettini & Cooke (2012)	3.050	20.392 ± 0.003	-1.92 O	2.51 ± 0.05	2.19 ± 0.02
Cooke et al. (2014), O'Meara et al. (2001)	2.537	19.4 ± 0.01	-1.77 O	2.58 ± 0.15	2.16 ± 0.04
Cooke et al. (2014), Pettini et al. (2008)	2.618	20.3 ± 0.01	-2.40 O	2.53 ± 0.10	2.18 ± 0.03
Cooke et al. (2014)	3.067	20.5 ± 0.01	-2.33 O	2.58 ± 0.07	2.16 ± 0.03
Cooke et al. (2014), O'Meara et al. (2006)	2.702	20.7 ± 0.05	-1.55 O	2.40 ± 0.14	2.25 ± 0.03
Riemer-Sørensen et al. (2015)	3.255	18.1 ± 0.03	-1.87 O	2.45 ± 0.28	2.23 ± 0.16
Balashov et al. (2016)	2.437	19.98 ± 0.01	-2.04 O	1.97 ± 0.33	2.54 ± 0.26
This work	3.572	17.925 ± 0.006	-2.26 O	2.62 ± 0.05	2.14 ± 0.03
Weighted average ¹	—	—	—	2.55 ± 0.03	2.17 ± 0.03
Unweighted average ¹	—	—	—	2.53 ± 0.17	2.18 ± 0.08
Planck Collaboration et al. (2016)	—	—	—	2.45 ± 0.05	2.225 ± 0.016

The conversion between D I/H I and $\Omega_b h^2$ is based on nuclear rates from Coc et al. (2015) for standard Big Bang Nucleosynthesis. ¹Without the Balashov et al. (2016) and Noterdaeme et al. (2012) measurements

Figure: Riemer-Sørensen et al. (MNRAS 468, 3239)

D/H measurement

- Lyman Series:

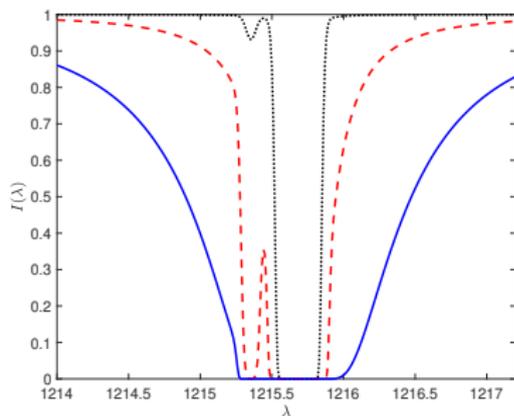
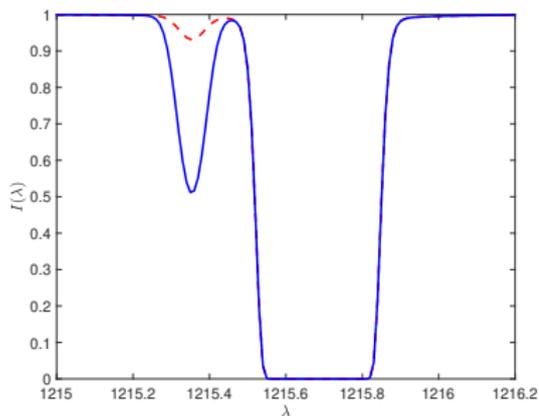
$$E_n = \frac{\mu e^4}{2(4\pi\epsilon_0\hbar)^2} \frac{1}{n^2} \quad \text{and} \quad \mu = \frac{Mm_e}{M + m_e},$$

where n is the principle quantum number, m_e and M are the mass of electron and nucleus.

- Hydrogen and Deuterium: $\mu_H = \frac{1836}{1+1836}$ and $\mu_D = \frac{3670}{1+3670}$
- Lyman α : $\lambda_H = 1215.67 \text{ \AA}$, $\lambda_D = 1215.34 \text{ \AA}$

D/H measurement

- Lyman α : $\lambda_H = 1215.67 \text{ \AA}$, $\lambda_D = 1215.34 \text{ \AA}$
- Left: $n_H = 10^{16}/\text{cm}^2$, $n_D/n_H = 10^{-3}$ (solid), 10^{-4} (dashed)
- Right: $n_H = 10^{16}$ (dotted), 10^{18} (dashed) and 10^{19} (solid) with $n_D/n_H = 10^{-4}$



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Voigt Function

- Cross-section of a two-level system:

$$\sigma(\nu) = cf \sqrt{\frac{3\pi\sigma_T}{8}} \phi(\nu),$$

where ν is the incoming photon energy, f is the oscillator strength, $\phi(\nu)$ is the Lorentzian

$$\phi(\nu) = \frac{\Gamma/4\pi^2}{(\nu - \nu_0)^2 + (\Gamma/4\pi)^2},$$

$E = h\nu_0$, and Γ is the spontaneous decay rate.

Voigt Function

- Doppler effect: $\nu_0 \rightarrow \nu_0 \left(1 + \frac{v_z}{c}\right)$
- Boltzmann distribution: $N(v_z) = \frac{\exp(-v_z^2/(2kT/m))}{\sqrt{2\pi kT/m}}$



Voigt Function

- Intensity Profile: $I_\nu = I_0 e^{-N\alpha_\nu}$, and

$$\alpha_\nu = \frac{\sqrt{\pi} e^2}{m_e c} \frac{f}{\Delta\nu_D} H(a, u),$$

where $\Delta\nu_D = \frac{b\nu_0}{c}$, $b = \sqrt{\frac{2kT}{m}}$, $u = \frac{(\nu - \nu_0)}{\Delta\nu_D}$ and $a = \frac{\Gamma}{4\pi\Delta\nu_D}$.

- Voigt Function:

$$H(a, u) = \frac{a}{\pi} \int_{-\infty}^{\infty} \frac{e^{-y^2} dy}{(u - y)^2 + a^2}.$$

Voigt Function

- Absorption and Voigt Function:
 - Two-level system \Rightarrow Lorentzian profile
 - Convolution of Boltzmann and Lorentzian

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- Kramers-Heisenberg formula

$$\frac{d\sigma}{d\Omega} = r_0^2 \left(\frac{\nu'}{\nu} \right) \left| \delta_{if} \bar{\epsilon}^\alpha \bar{\epsilon}^{\alpha'} + \frac{2\pi m_e \nu_n f \nu_{ni}}{\hbar} \sum_n \left[\frac{(\vec{x} \cdot \bar{\epsilon}^{\alpha'}) f_n (\vec{x} \cdot \bar{\epsilon}^\alpha)_{ni}}{\nu_{ni} - \nu - i\Gamma_n/2} + \frac{(\vec{x} \cdot \bar{\epsilon}^\alpha) f_n (\vec{x} \cdot \bar{\epsilon}^{\alpha'})_{ni}}{\nu_{ni} + \nu'} \right] \right|^2,$$

where $\nu(\epsilon^\alpha)$ and $\nu'(\epsilon^{\alpha'})$ are the frequency (orientation) of the incoming and outgoing photon, and

$$\nu_{ab} = \frac{E_a - E_b}{h}.$$

Kramers-Heisenberg Formula

- Lyman α : $1s \rightarrow 2p \rightarrow 1s$

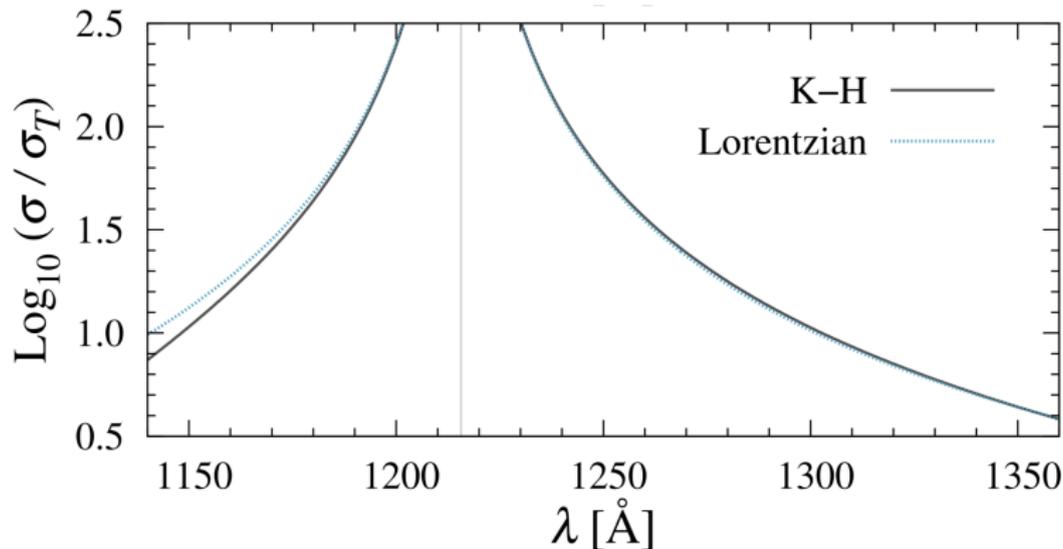


Figure: Kiehn Bach, Hee-Won Lee, JKAS 47, no.5, 187(2014)

Kramers-Heisenberg Formula

- Kramers-Heisenberg formula

$$\frac{d\sigma}{d\Omega} = r_0^2 \left(\frac{\nu'}{\nu} \right) \left| \delta_{if} \bar{\epsilon}^\alpha \bar{\epsilon}^{\alpha'} + \frac{2\pi m_e \nu_n f \nu_{ni}}{\hbar} \sum_n \left[\frac{(\vec{x} \cdot \bar{\epsilon}^{\alpha'}) f_n (\vec{x} \cdot \bar{\epsilon}^\alpha)_{ni}}{\nu_{ni} - \nu - i\Gamma_n/2} + \frac{(\vec{x} \cdot \bar{\epsilon}^\alpha) f_n (\vec{x} \cdot \bar{\epsilon}^{\alpha'})_{ni}}{\nu_{ni} + \nu'} \right] \right|^2.$$

- Rayleigh Scattering (Elastic): $1s \rightarrow np \rightarrow 1s$
- Raman Scattering (Inelastic): $1s \rightarrow np \rightarrow n's$ or $n'd$
- Example: $1s \rightarrow 4p \rightarrow$ Final states ($1s, 2s, 3s$ and $3d$)

Kramers-Heisenberg Formula

- $\sigma(\nu) = \sigma^{Rayleigh}(\nu) + \sum_f \sigma_f^{Raman}(\nu)$.
- Doppler effect: $\nu_{ni} \rightarrow \nu_{ni} \left(1 + \frac{v_z}{c}\right)$.
- Boltzmann distribution: $N(v_z) = \frac{\exp(-v_z^2/(2kT/m))}{\sqrt{2\pi kT/m}}$.

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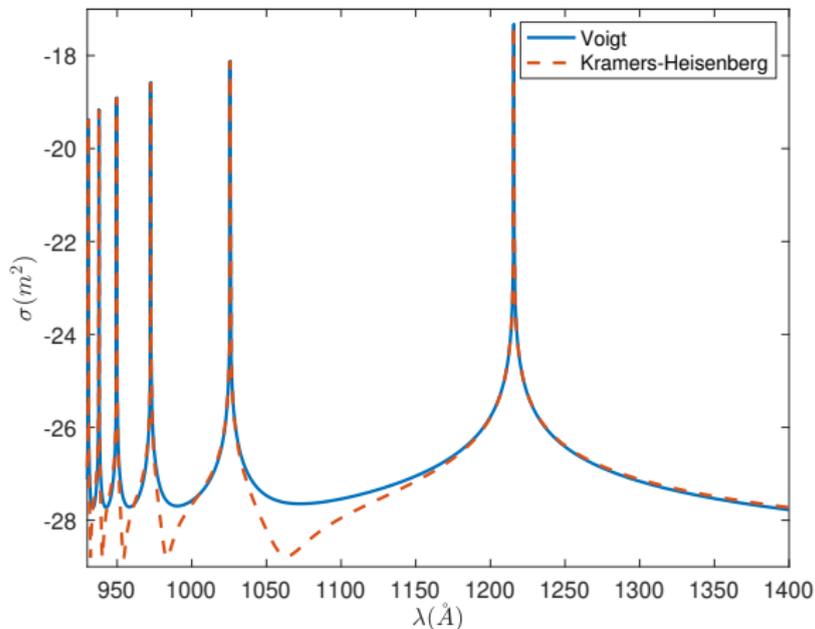
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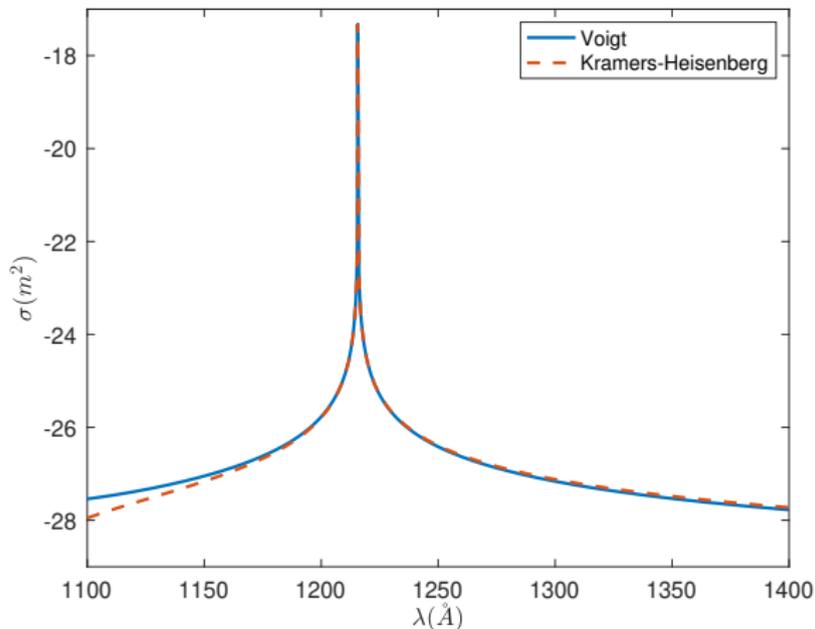
Cross Section

- Lyman Series:



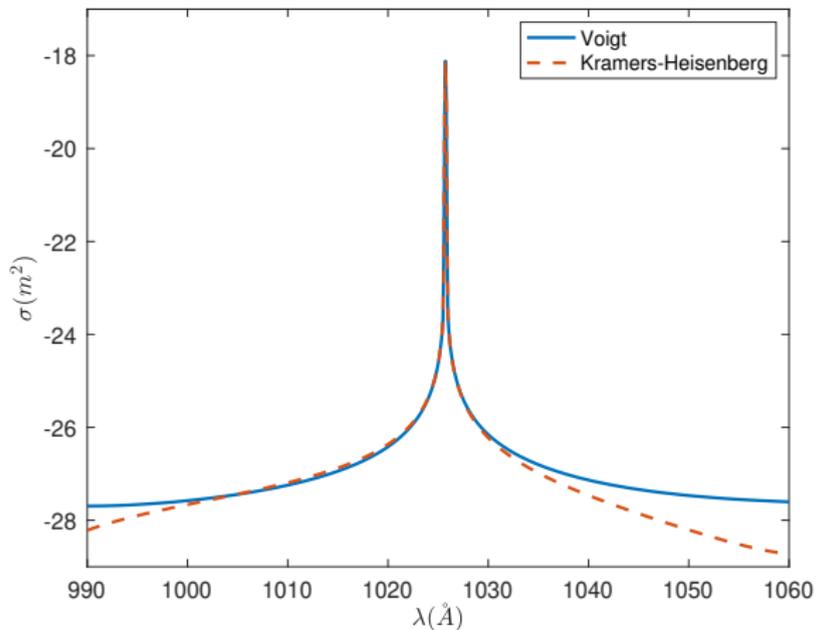
Cross Section

- Lyman α :



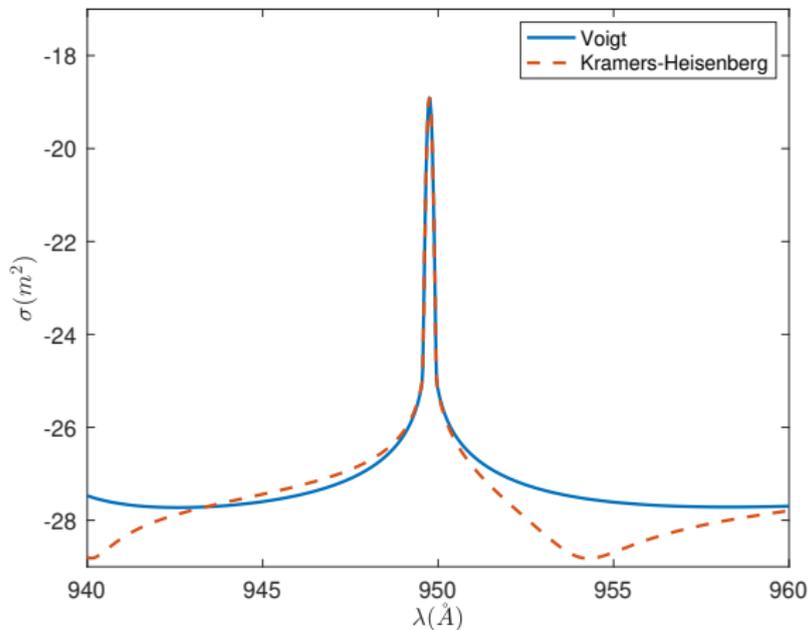
Cross Section

- Lyman β :



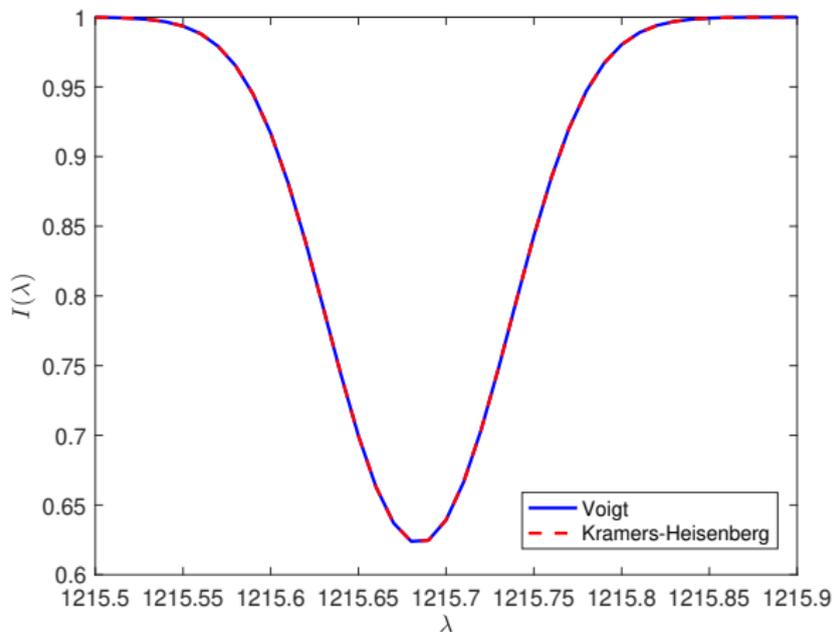
Cross Section

- Lyman γ :



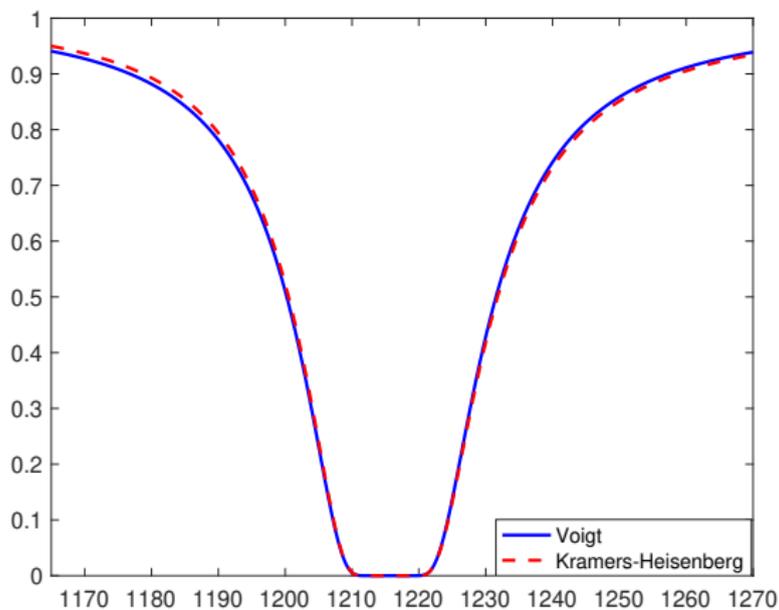
Intensity

- Lyman α with $\log N = 13.0$:



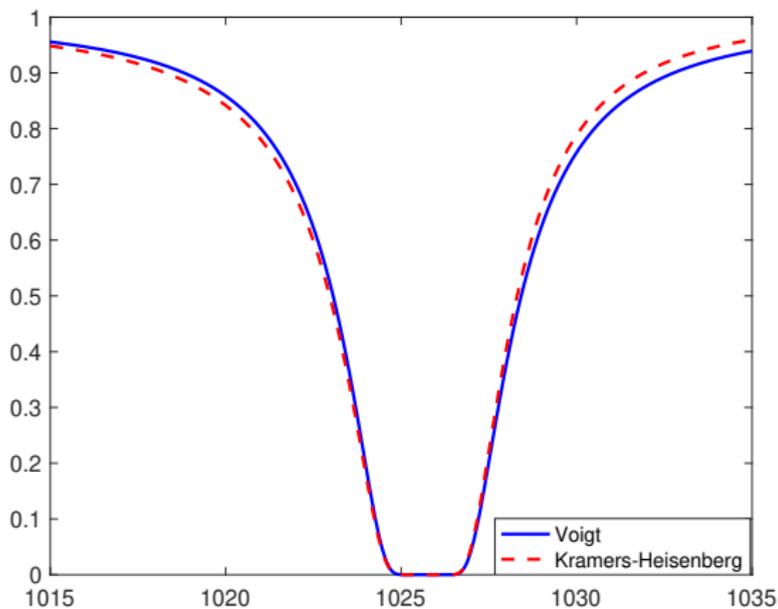
Intensity

- Lyman α with $\log N = 21.6$:



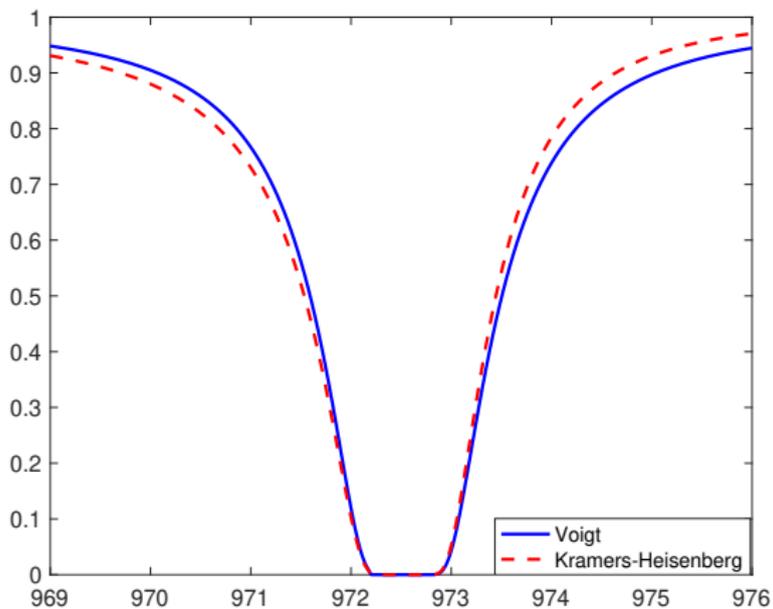
Intensity

- Lyman β with $\log N = 21.6$:



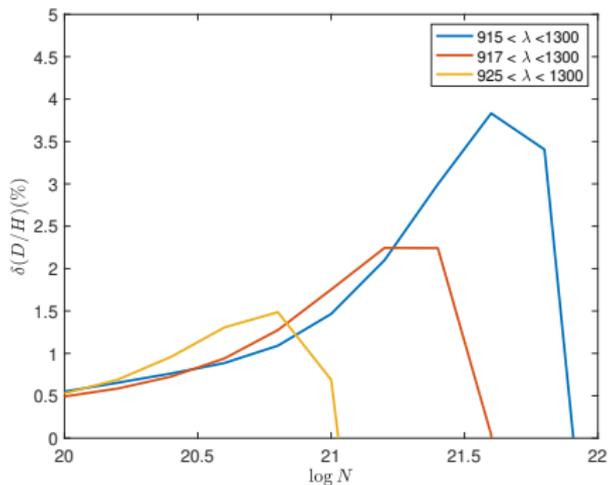
Intensity

- Lyman γ with $\log N = 21.6$:



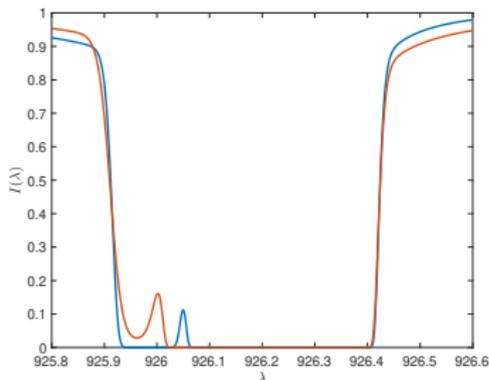
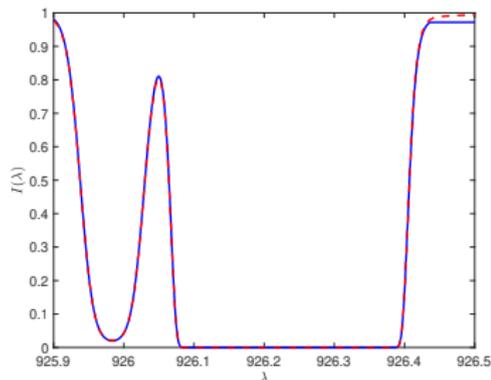
Fitting

- $\delta(D/H) \equiv \frac{n_{voigt-fit}}{n_{fid}} - 1$
- Fitting Region:
 - blue: Ly α - Ly14
 - red: Ly α - Ly12
 - yellow: Ly α - Ly7



Fitting

- Fit the fiducial with Ly α - Ly7
 - Left: Lyman 7 ($n = 1 \rightarrow 8$) with $\log N = 20.6$
 - Right: Lyman 7 ($n = 1 \rightarrow 8$) with $\log N = 21.6$



Summary

- Deuterium Abundance

- QSO: $D/H = (2.55 \pm 0.03) \times 10^{-5}$
- CMB: $D/H = (2.45 \pm 0.05) \times 10^{-5}$

- Speed:

- Voigt Profile: quick!!
- Karmers-Heisenberg: slow!!